

Package ‘DFA’

May 7, 2026

Type Package

Title Detrended Fluctuation Analysis

Version 1.0.0

Author Victor Barreto Mesquita[aut,cre], Paulo Canas Rodrigues[ctb], Florêncio Mendes Oliveira Filho[ctb], Ian Meneghel Danilevicz[ctb].

Maintainer Victor Barreto Mesquita <victormesquita40@hotmail.com>

Description Containing the Detrended Fluctuation Analysis (DFA), Detrended Cross-Correlation Analysis (DCCA), Detrended Cross-Correlation Coefficient (rhoDCCA), Delta Amplitude Detrended Cross-Correlation Coefficient (DeltarhoDCCA), log amplitude Detrended Fluctuation Analysis (DeltalogDFA), and the Activity Balance Index, it also includes two DFA automatic methods for identifying crossover points and a Deltalog automatic method for identifying reference channels.

License Apache License (== 2.0)

Encoding UTF-8

LazyData true

Depends stats, R (>= 3.5.0)

RoxygenNote 7.3.1

BugReports <https://github.com/victormesquita40/DFA/issues>

NeedsCompilation no

Repository CRAN

Date 2024-02-22

Language en-US

Date/Publication 2024-02-22 05:42:31 UTC

Contents

ABI	2
AUC	3
DCCA	4
DeltaDFA	6

Deltarho	8
DFA	10
DFA_aux	12
EEGsignal	13
euclidean	14
IXIC2008	15
lrcorrelation	16
LSE.L2008	17
NYA2008	18
rhoDCCA	19
secant	21
SSEC2008	22
SSP	23

Index	25
--------------	-----------

ABI	<i>Activity balance index (ABI)</i>
-----	-------------------------------------

Description

This function estimates the Activity balance index (ABI), which is a transformation of the self-similarity parameter (SSP), also known as scaling exponent or alpha.

Usage

ABI(x)

Arguments

x the estimated self-similarity parameter (SSP)

Details

$ABI = \exp(-\text{abs}(SSP-1)/\exp(-2))$

Value

The estimated Activity balance index (ABI) is a real number between zero and one.

Author(s)

Ian Meneghel Danilevicz

References

Danilevicz, I.M., van Hees, V.T., van der Heide, F., Jacob, L., Landré, B., Benadjaoud, M.A., Sabia, S. (2023). Measures of fragmentation of rest activity patterns: mathematical properties and interpretability based on accelerometer real life data. Research square. 10.21203/rs.3.rs-3543711/v1.

Examples

```
# Estimate Activity balance index of a very known time series available on R base: the sunspot.year.  
  
library(DFA)  
alpha = SSP(sunspot.year, scale = 1.2)  
abi = ABI(alpha)
```

AUC

Area Under the Curve

Description

Applies the Area Under the Curve on the log-log curve.

Usage

```
AUC(x, data)
```

Arguments

x	Vector of the decimal logarithm of the boxes sizes.
data	A data frame of different decimal logarithm of the DFA calculated in each boxe.

Details

Compute the Area Under the Curve to a data frame. The method returns the curve with higher AUC.

Value

position	Position of the DFA curve with higher Area Under the Curve (AUC).
Area	Respective Area Under the Curve (AUC) computed by trapezoidal rule for the channel with higher AUC.

Note

All of log-log curve contained in the data frame must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

<https://www.khanacademy.org/math/ap-calculus-ab/ab-integration-new/ab-6-2/a/understanding-the-trapezoidal-rule>
https://en.wikipedia.org/wiki/Trapezoidal_rule

Examples

Example with a data frame with different DFA exponents ranging from short 0.1 to long 0.9.
The functions returns the channel with higher AUC and its respective area.

```
library(DFA)
#library(latex2exp) # it is necessary for legend of the plot function

data("lrcorrelation")

#plot(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.9))`
#   ,xlab=TeX("$\log_{10}(n)$"),ylab=TeX("$\log_{10}F_{DFA}(n)$"),col="black"
#   ,pch=19, ylim= c(-0.8,1.2))
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.8))`,type="p"
#   ,col="blue", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.7))`,type="p"
#   ,col="red", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.6))`,type="p"
#   ,col="green", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.5))`,type="p"
#   ,col="brown", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.4))`,type="p"
#   ,col="yellow", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.3))`,type="p"
#   ,col="orange", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.2))`,type="p"
#   ,col="pink", pch=19)
#lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.1))`,type="p"
#   ,col="magenta", pch=19)

#legend("bottom", legend=c(TeX("$\alpha_{DFA} = 0.9$"),TeX("$\alpha_{DFA} = 0.8$")
#   ,TeX("$\alpha_{DFA} = 0.7$"),TeX("$\alpha_{DFA} = 0.6$")
#   ,TeX("$\alpha_{DFA} = 0.5$"),TeX("$\alpha_{DFA} = 0.4$")
#   ,TeX("$\alpha_{DFA} = 0.3$"),TeX("$\alpha_{DFA} = 0.2$")
#   ,TeX("$\alpha_{DFA} = 0.1$"))
#   , col=c("black", "blue", "red", "green", "brown", "yellow", "orange", "pink", "magenta")
#   , pch=c(19,19,19,19,19,19,19,19,19)
#   , cex = 0.55
#   , ncol = 5
#)

x = lrcorrelation$log10(boxes)`

data = lrcorrelation

AUC(x,data)
```

Description

Applies the Detrended Cross-Correlation Analysis (DCCA) to nonstationary time series.

Usage

```
DCCA(file,file2,scale = 2^(1/8),box_size = 4,m=1)
```

Arguments

file	Univariate time series (must be a vector or data frame)
file2	Univariate time series (must be a vector or data frame)
scale	Specifies the ratio between successive box sizes (by default scale = $2^{(1/8)}$)
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
m	An integer of the polynomial order for the detrending (by default m=1).

Details

The Detrended Cross-Correlation Analysis method (DCCA) can be computed in a geometric scale or for different choices of boxes sizes.

Value

boxe	Size n of the overlapping boxes.
DFA1	DFA of the first time series (file).
DFA2	DFA of the second time series (file2).
DCCA	Detrended Cross-Correlation function.

Note

The time series file and file2 must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

- N. Xu, P. Shang, S. Kamae Modeling traffic flow correlation using DFA and DCCA Nonlinear Dynam., 61 (2010), pp. 207-216
- B. Podobnik, D. Horvatic, A. Petersen, H.E. Stanley Cross-correlations between volume change and price change PNAS, 106 (52) (2009), pp. 22079-22084
- R. Ursilean, A.-M. Lazar Detrended cross-correlation analysis of biometric signals used in a new authentication method Electr. Electron. Eng., 1 (2009), pp. 55-58

Examples

```
#The following examples using the database of financial time series
#collected during the United States bear market of 2007-2009.
```

```
library(DFA)
data("NYA2008")
data("IXIC2008")
file = NYA2008
file2= IXIC2008
```

```
DCCA(file,file2,scale = 2^(1/8),box_size = c(4,8,16),m=1)
```

```
# Example with different polynomial fit order.
```

```
library(DFA)
data("NYA2008")
data("LSE.L2008")
file = NYA2008
file2= LSE.L2008
```

```
DCCA(file,file2,scale = 2^(1/8),box_size = c(4,8,16),m=2)
```

```
# Example using different choice of overlapping boxes sizes.
```

```
library(DFA)
data("NYA2008")
data("IXIC2008")
file = NYA2008
file2= IXIC2008
```

```
DCCA(file,file2,scale = "F",box_size = c(4,8,16),m=1)
```

DeltaDFA

log-amplitude Detrended Fluctuation Analysis (DeltaDFA)

Description

Applies the log-amplitude Detrended Fluctuation Analysis (DFA) to nonstationary time series.

Usage

```
DeltaDFA(file,file2,scale = 2^(1/8),box_size = 4,m=1)
```

Arguments

file Univariate time series (must be a vector or data frame)

file2	Univariate time series (must be a vector or data frame)
scale	Specifies the ratio between successive box sizes (by default scale = $2^{(1/8)}$)
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
m	An integer of the polynomial order for the detrending (by default m=1).

Details

The DFA log-amplitude fluctuation can be computed in a geometric scale or for different choices of boxes sizes.

Value

boxe	Size n of the overlapping boxes.
DeltaDFA	log-amplitude Detrended Fluctuation function defined as the difference between the DFA decimal logarithmic of the first time series (file) and the DFA decimal logarithmic of the second time series (file2)

Note

The time series file and file2 must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

- G. F. Zebende, F. M. Oliveira Filho, J. A. L. Cruz, Auto-correlation in the motor/imaginary human eeg signals: A vision about the dfafuctuations, PloS one 12 (9) (2017).
- F. Oliveira Filho, J. L. Cruz, G. Zebende, Analysis of the eeg bio-signals during the reading task by dfa method, Physica A: Statistical Mechanics and its Applications 525 (2019) 664-671.
- S. R. Hirekhan, R. R. Manthalkar, The detrended fluctuation and cross-correlation analysis of eeg signals, International Journal of Intelligent Systems Design and Computing 2 (2) (2018) .

Examples

```
#The following examples using the database of financial time series
#collected during the United States bear market of 2007-2009.

library(DFA)
data("NYA2008")
data("IXIC2008")
file = NYA2008
file2= IXIC2008

DeltaDFA(file,file2,scale = 2^(1/8),box_size = c(4,8,16),m=1)

# Example with different polynomial fit order.
```

```

library(DFA)
data("NYA2008")
data("LSE.L2008")
file = NYA2008
file2= LSE.L2008

DeltaDFA(file,file2,scale = 2^(1/8),box_size = c(4,8,16),m=2)

# Example using different choice of overlapping boxes sizes.

library(DFA)
data("NYA2008")
data("IXIC2008")
file = NYA2008
file2= IXIC2008

DeltaDFA(file,file2,scale = "F",box_size = c(4,8,16),m=1)

```

Deltarho	<i>Delta Amplitude</i>	<i>Detrended</i>	<i>Cross-Correlation</i>	<i>Coefficient</i>
----------	------------------------	------------------	--------------------------	--------------------

(DeltarhoDCCA)

Description

Applies the Detrended Cross-Correlation Coefficient Difference (Deltarho) to nonstationary time series.

Usage

```
Deltarho(file,file2,file3,file4,scale = 2^(1/8),box_size = 4,m=1)
```

Arguments

file	Univariate time series (must be a vector or data frame)
file2	Univariate time series (must be a vector or data frame)
file3	Univariate time series (must be a vector or data frame)
file4	Univariate time series (must be a vector or data frame)
scale	Specifies the ratio between successive box sizes (by default scale = $2^{(1/8)}$)
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
m	An integer of the polynomial order for the detrending (by default m=1).

Details

The Deltarho can be computed in a geometric scale or for different choices of boxes sizes.

Value

boxe	Size n of the overlapping boxes.
DFA1	DFA of the first time series (file).
DFA2	DFA of the second time series (file2).
DFA3	DFA of the third time series (file3).
DFA4	DFA of the fourth time series (file4).
DCCA	Detrended Cross-Correlation function between the first time series (file) and the second time series (file2).
DCCA2	Detrended Cross-Correlation function between the third time series (file3) and the fourth time series (file4).
rhoDCCA	Detrended Cross-Correlation Coefficient function, defined as the ratio between the DCCA and two DFA (DFA1, DFA2).
rhoDCCA2	Detrended Cross-Correlation Coefficient function, defined as the ratio between the DCCA2 and two DFA (DFA3, DFA4).

Note

The time series file,file2,file3 and file4 must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

SILVA, Marcus Fernandes da et al. Quantifying cross-correlation between ibovespa and brazilian blue-chips: The dcca approach. *Physica A: Statistical Mechanics and its Applications*, v. 424,2015.

Examples

```
#The following examples using the database of financial time series
#collected during the United States bear market of 2007-2009.

library(DFA)
data("NYA2008")
data("IXIC2008")
data("LSE.L2008")
data("SSEC2008")

file = NYA2008
file2= IXIC2008
file3 = LSE.L2008
file4 = SSEC2008

Deltarho(file,file2,file3,file4,scale = 2^(1/8),box_size = c(4,8,16),m=1)

# Example with different polynomial fit order.
```

```

library(DFA)
data("NYA2008")
data("IXIC2008")
data("LSE.L2008")
data("SSEC2008")

file = NYA2008
file2 = LSE.L2008
file3= IXIC2008
file4 = SSEC2008

Deltarho(file,file2,file3,file4,scale = 2^(1/8),box_size = c(4,8,16),m=2)

# Example using different choice of overlapping boxes sizes.

library(DFA)
data("NYA2008")
data("IXIC2008")
data("LSE.L2008")
data("SSEC2008")

file = NYA2008
file2= IXIC2008
file3 = LSE.L2008
file4 = SSEC2008

Deltarho(file,file2,file3,file4,scale = "F",box_size = c(4,8,16),m=1)

```

DFA

Detrended Fluctuation Analysis (DFA)

Description

Applies the Detrended Fluctuation Analysis (DFA) to nonstationary time series.

Usage

```
DFA(file,scale = 2^(1/8),box_size = 4,m=1)
```

Arguments

file	Univariate time series (must be a vector or data frame)
scale	Specifies the ratio between successive box sizes (by default scale = $2^{(1/8)}$)
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
m	An integer of the polynomial order for the detrending (by default m=1).

Details

The DFA fluctuation can be computed in a geometric scale or for different choices of boxes sizes.

Value

boxe	Size n of the overlapping boxes.
DFA	Detrended Fluctuation function.

Note

The time series file and file2 must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

C.-K. Peng, S.V. Buldyrev, S. Havlin, M. Simons, H.E. Stanley, A.L. Goldberger Phys. Rev. E, 49 (1994), p. 1685

H.E. Stanley, L.A.N. Amaral, A.L. Goldberger, S. Havlin, P.Ch. Ivanov, C.-K. Peng Physica A, 270 (1999), p. 309

P.C. Ivanov, A. Bunde, L.A.N. Amaral, S. Havlin, J. Fritsch-Yelle, R.M. Baevsky, H.E. Stanley, A.L. Goldberger Europhys. Lett., 48 (1999), p. 594

P. Talkner, R.O. Weber Phys. Rev. E, 62 (2000), p. 150

M. Ausloos, K. Ivanova Physica A, 286 (2000), p. 353

H.E. Hurst, R.P. Black, Y.M. Simaika Long-Term Storage, An Experimental Study, Constable, London (1965)

Examples

```
#The following examples using the database of financial time series
#collected during the United States bear market of 2007-2009.
```

```
library(DFA)
data("NYA2008")
file = NYA2008
```

```
DFA(file,scale = 2^(1/8),box_size = c(4,8,16),m=1)
```

```
# Example with different polynomial fit order.
```

```
library(DFA)
data("LSE.L2008")
file = LSE.L2008
```

```
DFA(file,scale = 2^(1/8),box_size = c(4,8,16),m=2)
```

```
# Example using different choice of overlapping boxes sizes.

library(DFA)
data("NYA2008")
file = NYA2008

DFA(file,scale = "F",box_size = c(4,8,16),m=1)
```

DFA_aux

Detrended Fluctuation Analysis Auxiliary function

Description

Function, which is used as an auxiliary function with DFA, to store data between each iteration and thus decrease the computation time speed to compute the alpha coefficient.

Usage

```
DFA_aux(j, box_size, ninbox2, file, y_k, m, N)
```

Arguments

j	J-th iteration
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
ninbox2	The number of windows
file	Univariate time series (must be a vector or data frame)
y_k	Vector with the fit's output stored.
m	An integer of the polynomial order for the detrending (by default m=1).
N	The time series size

Details

The DFA fluctuation can be computed in a geometric scale or for different choices of boxes sizes.

Value

boxe	Size n of the overlapping boxes.
DFA	Detrended Fluctuation function.

Note

The time series file and file2 must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

- C.-K. Peng, S.V. Buldyrev, S. Havlin, M. Simons, H.E. Stanley, A.L. Goldberger Phys. Rev. E, 49 (1994), p. 1685
- H.E. Stanley, L.A.N. Amaral, A.L. Goldberger, S. Havlin, P.Ch. Ivanov, C.-K. Peng Physica A, 270 (1999), p. 309
- P.C. Ivanov, A. Bunde, L.A.N. Amaral, S. Havlin, J. Fritsch-Yelle, R.M. Baeovsky, H.E. Stanley, A.L. Goldberger Europhys. Lett., 48 (1999), p. 594
- P. Talkner, R.O. Weber Phys. Rev. E, 62 (2000), p. 150
- M. Ausloos, K. Ivanova Physica A, 286 (2000), p. 353
- H.E. Hurst, R.P. Black, Y.M. Simaika Long-Term Storage, An Experimental Study, Constable, London (1965)

Examples

```
#There is not directy usage of this function,  
# because it must be used in parallel with the DFA function.
```

EEGsignal

A single DFA dataframe with the decimal log fluctuation curve.

Description

The data contains the log fluctuation channel curve calculated for an epileptic subject extracted in the Physionet platform.

Usage

```
data("EEGsignal")
```

Format

A data frame with 91 observations on the following 2 variables.

‘log10(boxes)’ a numeric vector referring to the decimal logarithm of the boxes sizes.

‘log10(DFA)’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) calculated in each boxe.

References

<https://physionet.org/content/chbmit/1.0.0/chb01/#files-panel>

Examples

```
data(EEGsignal)
data("EEGsignal")
x<-EEGsignal$log10(boxes)
y<-EEGsignal$log10(DFA)
plot(x,y)
```

 euclidean

euclidean method for detection of crossover points

Description

Applies the euclidean method for detection of crossover points on the log-log curve.

Usage

```
euclidean(x,y,npoint)
```

Arguments

x	Vector of the decimal logarithm of the boxes sizes.
y	Vector of the decimal logarithm of the DFA calculated in each boxe.
npoint	Number of crossover points calculated on the log-log curve.

Value

position	Position of the crossover point identified by the euclidean method.
sugestion_before	Sugestion for the position of the second crossover point identified by the euclidean method and calculated in the area before the first crossover point.
sugestion_after	Sugestion for the position of the second crossover point identified by the euclidean method and calculated in the area after the first crossover point.

Author(s)

Victor Barreto Mesquita

References

https://en.wikipedia.org/wiki/Distance_from_a_point_to_a_line

Examples

```
# Example with crossover point fixed in position=20.

library(DFA)
data(lrcorrelation)
x<-lrcorrelation$log10(boxes)^
y<-c(lrcorrelation$log10(DFA(alpha = 0.1))^[1:20],lrcorrelation$log10(DFA(alpha = 0.3))^[21:40])
plot(x,y,xlab="log10(boxes)",ylab="log10(DFA)",pch=19)
fit<- lm(y[1:20] ~ x[1:20])
fit2<-lm(y[21:40] ~ x[21:40])
abline(fit,col="blue")
abline(fit2,col="red")
euclidean(x,y,npoint=1)

# Example with crossover point fixed in position=13 and 26.
library(DFA)
data(lrcorrelation)
x<-lrcorrelation$log10(boxes)^
y<-c(lrcorrelation$log10(DFA(alpha = 0.2))^[1:13],lrcorrelation$log10(DFA(alpha = 0.6))^[14:26]
,lrcorrelation$log10(DFA(alpha = 0.9))^[27:40])
plot(x,y,xlab="log10(boxes)",ylab="log10(DFA)",pch=19)
fit<- lm(y[1:13] ~ x[1:13])
fit2<-lm(y[14:26] ~ x[14:26])
fit3<-lm(y[27:40] ~ x[27:40])
abline(fit,col="blue")
abline(fit2,col="red")
abline(fit3,col="brown")
euclidean(x,y,npoint=2)
```

IXIC2008

Time series referring to the adjusted closing price of the NASDAQ Composite (^IXIC) during the United States bear market of 2007–2009

Description

Univariate vector of time series referring to the adjusted closing price of the NASDAQ Composite (^IXIC) during the United States bear market of 2007–2009, considered the worst bear market this side of the Great Depression. The crash, which unfolded from Oct. 9, 2007 to March 9, 2009, obliterated more than half of the total value of the U.S. stock market. During this period, the S&P 500 lost approximately a half of its value and threatened the very existence of iconic companies from General Motors to Merrill Lynch.

Usage

```
data("IXIC2008")
```

Format

The format is: num [1:332] 2811 2772 2805 2780 2763 ...

Source

Yahoo Finance

References

<https://www.investopedia.com/terms/b/bearmarket.asp>

Examples

```
library(DFA)
data("IXIC2008")
```

Ircorrelation	<i>data frame with log fluctuation channel curve simulated following an ARFIMA process</i>
---------------	--

Description

The data contains the data frame with log fluctuation channel curve simulated following an ARFIMA process with different DFA exponents ranging from short 0.1 to long 0.9 .

Usage

```
data("Ircorrelation")
```

Format

A data frame with 40 observations on the following 10 variables.

- ‘log10(boxes)’ a numeric vector referring to the decimal logarithm of the boxes sizes.
- ‘log10(DFA(alpha = 0.1))’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.1 and calculated in each boxe.
- ‘log10(DFA(alpha = 0.2))’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.2 and calculated in each boxe.
- ‘log10(DFA(alpha = 0.3))’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.3 and calculated in each boxe.
- ‘log10(DFA(alpha = 0.4))’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.4 and calculated in each boxe.
- ‘log10(DFA(alpha = 0.5))’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.5 and calculated in each boxe.
- ‘log10(DFA(alpha = 0.6))’ a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.6 and calculated in each boxe.

'log10(DFA(alpha = 0.7))' a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.7 and calculated in each boxe.

'log10(DFA(alpha = 0.8))' a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.8 and calculated in each boxe.

'log10(DFA(alpha = 0.9))' a numeric vector referring to the decimal logarithm of the Detrended Fluctuation Analysis (DFA) with DFA exponent equal 0.9 and calculated in each boxe.

Examples

```
library(DFA)
#library(latex2exp) # it is necessary for legend of the plot function
data(lrcorrelation)
plot(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.9))`
      ,xlab="log10(n)",ylab="log10FDFA(n)",col="black"
      ,pch=19, ylim= c(-0.8,1.2))
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.8))`,type="p"
      ,col="blue", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.7))`,type="p"
      ,col="red", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.6))`,type="p"
      ,col="green", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.5))`,type="p"
      ,col="brown", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.4))`,type="p"
      ,col="yellow", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.3))`,type="p"
      ,col="orange", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.2))`,type="p"
      ,col="pink", pch=19)
lines(lrcorrelation$log10(boxes),lrcorrelation$log10(DFA(alpha = 0.1))`,type="p"
      ,col="magenta", pch=19)

#legend("bottom", legend=c(TeX("$\\alpha_{DFA} = 0.9$"),TeX("$\\alpha_{DFA} = 0.8$")
#                          ,TeX("$\\alpha_{DFA} = 0.7$"),TeX("$\\alpha_{DFA} = 0.6$")
#                          ,TeX("$\\alpha_{DFA} = 0.5$"),TeX("$\\alpha_{DFA} = 0.4$")
#                          ,TeX("$\\alpha_{DFA} = 0.3$"),TeX("$\\alpha_{DFA} = 0.2$")
#                          ,TeX("$\\alpha_{DFA} = 0.1$"))
#      , col=c("black", "blue", "red", "green", "brown", "yellow", "orange", "pink", "magenta")
#      , pch=c(19,19,19,19,19,19,19,19,19)
#      , cex = 0.55
#      , ncol = 5
#)
```

Description

Univariate vector of time series referring to the adjusted closing price of the London Stock Exchange Group plc (LSE.L) during the period which the United States faced the bear market of 2007–2009, considered the worst bear market this side of the Great Depression. The crash, which unfolded from Oct. 9, 2007 to March 9, 2009, obliterated more than half of the total value of the U.S. stock market. During this period, the S&P 500 lost approximately a half of its value and threatened the very existence of iconic companies from General Motors to Merrill Lynch.

Usage

```
data("LSE.L2008")
```

Format

The format is: num [1:332] 1172 1176 1165 1163 1163 ...

Source

Yahoo Finance

References

<https://www.investopedia.com/terms/b/bearmarket.asp>

Examples

```
library(DFA)
data("LSE.L2008")
```

NYA2008

Time series referring to the adjusted closing price of the NYSE COMPOSITE (^NYA) during the United States bear market of 2007–2009

Description

Univariate vector of time series referring to the adjusted closing price of the NYSE COMPOSITE (^NYA) during the United States bear market of 2007–2009, considered the worst bear market this side of the Great Depression. The crash, which unfolded from Oct. 9, 2007 to March 9, 2009, obliterated more than half of the total value of the U.S. stock market. During this period, the S&P 500 lost approximately a half of its value and threatened the very existence of iconic companies from General Motors to Merrill Lynch.

Usage

```
data("NYA2008")
```

Format

The format is: num [1:332] 10264 10245 10301 10216 10125 ...

Source

Yahoo Finance

References

<https://www.investopedia.com/terms/b/bearmarket.asp>

Examples

```
library(DFA)
data("NYA2008")
```

rhoDCCA

Detrended Cross-Correlation Coefficient (rhoDCCA)

Description

Applies the Detrended Cross-Correlation Coefficient (rhoDCCA) to nonstationary time series.

Usage

```
rhoDCCA(file,file2,scale = 2^(1/8),box_size = 4,m=1)
```

Arguments

file	Univariate time series (must be a vector or data frame)
file2	Univariate time series (must be a vector or data frame)
scale	Specifies the ratio between successive box sizes (by default scale = $2^{(1/8)}$)
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
m	An integer of the polynomial order for the detrending (by default m=1).

Details

The Detrended Cross-Correlation Coefficient (rhoDCCA) can be computed in a geometric scale or for different choices of boxes sizes.

Value

boxe	Size n of the overlapping boxes.
DFA1	DFA of the first time series (file).
DFA2	DFA of the second time series (file2).
DCCA	Detrended Cross-Correlation function.
rhoDCCA	Detrended Cross-Correlation Coefficient function, defined as the ratio between the DCCA and two DFA (DFA1 ,DFA2).

Note

The time series file and file2 must have the same sample size.

Author(s)

Victor Barreto Mesquita

References

Zebende G.F. DCCA cross-correlation coefficient: Quantifying level of cross-correlation *Physica A*, 390 (4) (2011), pp. 614-618

Vassoler R.T., Zebende G.F. DCCA cross-correlation coefficient apply in time series of air temperature and air relative humidity *Physica A*, 391 (7) (2012), pp. 2438-2443

Guedes E.F., Zebende G.F., da Cunha Lima I.C. Quantificacao dos Efeitos do Cambio na Producao da Industria de Transformacao Baiana: uma abordagem via coeficiente de correlacao cruzada rho dcca *Conjuntura & Planejamento*, 1 (192) (2017), pp. 75-89

Examples

#The following examples using the database of financial time series
#collected during the United States bear market of 2007-2009.

```
library(DFA)
data("NYA2008")
data("IXIC2008")
file = NYA2008
file2= IXIC2008
```

```
rhoDCCA(file,file2,scale = 2^(1/8),box_size = c(4,8,16),m=1)
```

Example with different polynomial fit order.

```
library(DFA)
data("NYA2008")
data("LSE.L2008")
file = NYA2008
file2= LSE.L2008
```

```
rhoDCCA(file,file2,scale = 2^(1/8),box_size = c(4,8,16),m=2)
```

Example using different choice of overlapping boxes sizes.

```
library(DFA)
data("NYA2008")
data("IXIC2008")
file = NYA2008
file2= IXIC2008
```

```
rhoDCCA(file,file2,scale = "F",box_size = c(4,8,16),m=1)
```

secant	<i>secant method for detection of crossover points</i>
--------	--

Description

Applies the secant method for detection of crossover points on the log-log curve.

Usage

```
secant(x,y,npoint,size_fit)
```

Arguments

x	Vector of the decimal logarithm of the boxes sizes.
y	Vector of the decimal logarithm of the DFA calculated in each boxe.
npoint	Number of crossover points calculated on the log-log curve.
size_fit	Number of points of the two semi-curved fitted in the extremes of the log-log curve.

Value

position	Position of the crossover point identified by the secant method.
----------	--

Author(s)

Victor Barreto Mesquita

Examples

```
# Example with the data referring to the log fluctuation  
#channel curve data calculated for an epileptic subject  
#extracted in the Physionet platform.
```

```
library(DFA)  
data("EEGsignal")  
x<-EEGsignal$log10(boxes)`  
y<-EEGsignal$log10(DFA)`  
plot(x,y,xlab="log10(boxes)",ylab="log10(DFA)")
```

```
secant(x,y,npoint=2,size_fit=8)
```

```
# Example with crossover point fixed in position=20.
```

```
library(DFA)
```

```
part1 <- seq(1,20)
part2 <- seq(20,1)
y = c(part1,part2)
x<-seq(1,40)
plot(x,y)
secant(x,y,npoint=1,size_fit=8)
```

SSEC2008

Time series referring to the adjusted closing price of the SSE Composite Index (^SSEC) during the period which the United States faced the bear market of 2007–2009.

Description

Univariate vector of time series referring to the adjusted closing price of the SSE Composite Index (^SSEC) during the period which the United States faced the bear market of 2007–2009, considered the worst bear market this side of the Great Depression. The crash, which unfolded from Oct. 9, 2007 to March 9, 2009, obliterated more than half of the total value of the U.S. stock market. During this period, the S&P 500 lost approximately a half of its value and threatened the very existence of iconic companies from General Motors to Merrill Lynch.

Usage

```
data("SSEC2008")
```

Format

The format is: num [1:332] 5771 5913 5903 6030 6092 ...

Source

Yahoo Finance

References

<https://www.investopedia.com/terms/b/bearmarket.asp>

Examples

```
library(DFA)
data("SSEC2008")
```

SSP *Self-similarity parameter (SSP)*

Description

This function estimates the self-similarity parameter (SSP), also known as scaling exponent or alpha.

Usage

```
SSP(file, scale = 2^(1/8), box_size = 4, m=1)
```

Arguments

file	Univariate time series (must be a vector or data frame)
scale	Specifies the ratio between successive box sizes (by default scale = $2^{(1/8)}$)
box_size	Vector of box sizes (must be used in conjunction with scale = "F")
m	An integer of the polynomial order for the detrending (by default m=1)

Details

The DFA fluctuation can be computed in a geometric scale or for different choices of boxes sizes.

Value

Estimated alpha is a real number between zero and two.

Note

It is not possible estimating alpha for multiple time series at once.

Author(s)

Ian Meneghel Danilevicz and Victor Barreto Mesquita

References

C.-K. Peng, S.V. Buldyrev, S. Havlin, M. Simons, H.E. Stanley, A.L. Goldberger Phys. Rev. E, 49 (1994), p. 1685

Mesquita, V., Filho, F., Rodrigues, P. (2020). Detection of crossover points in detrended fluctuation analysis: An application to EEG signals of patients with epilepsy. Bioinformatics. 10.1093/bioinformatics/btaa955.

Examples

```
# Estimate self-similarity of a very known time series available on R base: the sunspot.year.  
# Then the spend time with each method is compared.  
library(DFA)  
SSP(sunspot.year, scale = 2)  
SSP(sunspot.year, scale = 1.2)  
  
time1 = system.time(SSP(sunspot.year, scale = 1.2))  
time2 = system.time(SSP(sunspot.year, scale = 2))  
  
time1  
time2
```

Index

* datasets

- EEGsignal, [13](#)
- IXIC2008, [15](#)
- lrcorrelation, [16](#)
- LSE.L2008, [17](#)
- NYA2008, [18](#)
- SSEC2008, [22](#)

ABI, [2](#)

AUC, [3](#)

DCCA, [4](#)

DeltaDFA, [6](#)

Deltarho, [8](#)

DFA, [10](#)

DFA_aux, [12](#)

EEGsignal, [13](#)

euclidean, [14](#)

IXIC2008, [15](#)

lrcorrelation, [16](#)

LSE.L2008, [17](#)

NYA2008, [18](#)

rhoDCCA, [19](#)

secant, [21](#)

SSEC2008, [22](#)

SSP, [23](#)