

Package ‘scalednap’

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Type Package

Title Community Detection by Scaled Null-Adjusted Persistence

Version 1.0.0

Description Finds the vertex partition of an undirected graph that maximises a persistence-based objective, using the Milano local-search algorithm. Three related quality measures are supported: the persistence probability of a community, its null-adjusted persistence (NAP), and the scaled null-adjusted persistence (Scaled-NAP), which interpolates between NAP and modularity. The methods are described in Avellone et al. (2023) [<doi:10.1007/s10288-023-00559-z>](https://doi.org/10.1007/s10288-023-00559-z) and Avellone et al. (2025) [<doi:10.1016/j.ins.2025.123032>](https://doi.org/10.1016/j.ins.2025.123032).

License GPL (>= 2)

Encoding UTF-8

SystemRequirements C++20

URL <https://github.com/aavellone/scalednap-r>

BugReports <https://github.com/aavellone/scalednap-r/issues>

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'global_persistence.R' 'local_persistence.R'

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scalednap-package	<i>scalednap</i>
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Description

Given a non-oriented graph, calculates the optimal vertex partition using persistence as the objective function.

Details

See manual entries.

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cluster_milano	<i>cluster_milano</i>
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Description

Calculates the vertex partition with maximum global null-adjusted persistence. This function is polymorphic: it automatically detects the input type and accepts either a vertex vector (accompanied by an edge list) or directly an igraph object.

Usage

```
cluster_milano(x, ...)

## Default S3 method:
cluster_milano(
  x,
  edge_list,
  weights = NULL,
  membership = NULL,
  H0 = 0,
  seed = NULL,
  n_restarts = 1L,
  tol = NULL,
  max_level = 0L,
  num_threads = 1L,
  collect_stats = FALSE,
  ...
)

## S3 method for class 'igraph'
cluster_milano(
  x,
  membership = NULL,
  H0 = 0,
  seed = NULL,
  n_restarts = 1L,
  tol = NULL,
  max_level = 0L,
  num_threads = 1L,
  collect_stats = FALSE,
  ...
)
```

Arguments

<code>x</code>	An integer or character vector representing the graph vertices, OR an object of class <code>igraph</code> .
<code>...</code>	Additional arguments passed to specific methods (e.g., <code>edge_list</code> , <code>weights</code> , <code>tol</code> , <code>max_level</code> , etc.).
<code>edge_list</code>	Integer matrix with two columns representing the graph edge list.
<code>weights</code>	Numeric vector of positive edge weights. If <code>NULL</code> , all weights default to 1.
<code>membership</code>	Integer vector representing the starting partition: $x_i = k$ if i in C_k . If <code>NULL</code> , each vertex starts in its own cluster.
<code>H0</code>	Selects the quality measure. If <code>NULL</code> , the persistence probability is used. If 0 (default), the null-adjusted persistence (NAP). If a value in $(0, 1]$, the scaled null-adjusted persistence (Scaled-NAP, $sNAP_\alpha$), with scaling exponent α equal to <code>H0</code> .

seed	Two forms are accepted. A single non-negative integer is the <i>master seed</i> : if NULL or 0 a random master is generated (and reported in the result); if positive, the run is fully reproducible — the seeds of the individual restarts are derived deterministically from the master in C++ (SplitMix64 mixing, identical to the command-line tool). Alternatively, a digit string (e.g. the seed_winning field of a previous result) is an <i>exact 64-bit seed</i> used as-is, with no derivation: it reproduces that single restart and requires n_restarts = 1.
n_restarts	Positive integer: number of independent restarts (default 1). The best partition across restarts is returned; winning_restart in the result tells which one won.
tol	Optional numeric tolerance for the stopping criterion. If NULL (default), an adaptive threshold is calculated dynamically in C++.
max_level	Optional integer representing the maximum number of aggregation levels. If 0 (default) or NULL, the algorithm runs until convergence.
num_threads	Number of threads for the move-node phase. 1 (default) runs the deterministic sequential mode; values greater than 1 enable the lock-free parallel mode (Hogwild!), which is NOT deterministic even for a fixed seed.
collect_stats	Logical. If TRUE, the per-cluster scores are computed and returned in clusters_value. Default FALSE.

Value

A list with five elements:

membership The optimal vertex partition.

score The measure value of the optimal partition.

clusters_value Numeric vector with the score of each cluster, or NULL unless collect_stats = TRUE.

iterations Integer vector: number of move-node sweeps performed at each coarsening level.

seed The master seed actually used (numeric). Re-running with seed set to this value and the same n_restarts reproduces the result exactly. NA when the run was launched with an exact 64-bit seed string (no master exists in that case).

winning_restart 1-based index of the restart that produced the returned partition.

seed_winning Character string: the exact 64-bit seed used by the winning restart (returned as a string because R doubles are exact only up to 2^{53}). Pass it back as seed to reproduce that single winning run directly.

Examples

```
library(scalednap)

# --- EXAMPLE 1: Standard input (vectors and matrices) ---
edg <- c(1, 2, 1, 3, 1, 4, 2, 3, 3, 4, 4, 5, 5, 6, 5, 7, 6, 7)
edge_list <- matrix(edg, ncol = 2, byrow = TRUE)
vertex <- c(1, 2, 3, 4, 5, 6, 7)
cluster_milano(x = vertex, edge_list = edge_list)

# --- EXAMPLE 2: igraph input ---
```

```

if (requireNamespace("igraph", quietly = TRUE)) {
  g <- igraph::make_ring(10)
  cluster_milano(g)
}

```

global_persistence *global_persistence*

Description

Given a partition of the graph vertices, calculates the global persistence as the sum of the local persistences of the individual clusters. Persistence can be either null-adjusted or probability-based. This function is polymorphic: it automatically detects the input type and accepts either a vertex vector (accompanied by an edge list) or directly an igraph object.

Usage

```

global_persistence(x, ...)

## Default S3 method:
global_persistence(x, edge_list, weights = NULL, membership, H0 = 0, ...)

## S3 method for class 'igraph'
global_persistence(x, membership, H0 = 0, ...)

```

Arguments

<code>x</code>	An integer or character vector representing the graph vertices, OR an object of class <code>igraph</code> .
<code>...</code>	Additional arguments passed to specific methods (e.g., <code>edge_list</code> , <code>weights</code> , <code>membership</code> , <code>H0</code>).
<code>edge_list</code>	Integer matrix with two columns representing the graph edge list.
<code>weights</code>	Numeric vector of edge weights. If <code>NULL</code> , all weights default to 1.
<code>membership</code>	Integer vector of vertex cluster assignments: $x_i = k$ if i in C_k .
<code>H0</code>	Selects the quality measure. If <code>NULL</code> , the persistence probability is used. If <code>0</code> (default), the null-adjusted persistence (NAP). If a value in $(0, 1]$, the scaled null-adjusted persistence (Scaled-NAP, $sNAP_\alpha$), with scaling exponent α equal to <code>H0</code> .

Value

A list with two elements:

score The global persistence of the partition.

clusters_value The local persistence of each cluster. A value of `NaN` indicates that cluster C_k is empty in the input membership.

Examples

```
library(scalednap)

# --- EXAMPLE 1: Standard input (vectors and matrices) ---
edg <- c(1, 2, 1, 3, 1, 4, 2, 3, 3, 4, 4, 5, 5, 6, 5, 7, 6, 7)
edge_list <- matrix(edg, ncol = 2, byrow = TRUE)
vertex <- c(1, 2, 3, 4, 5, 6, 7)
mem <- c(1, 1, 1, 1, 2, 2, 2)
global_persistence(x = vertex, edge_list = edge_list, membership = mem)

# --- EXAMPLE 2: igraph input ---
if (requireNamespace("igraph", quietly = TRUE)) {
  g <- igraph::make_ring(10)
  mem <- c(rep(1, 5), rep(2, 5))
  global_persistence(g, membership = mem)
}
```

local_persistence	<i>local_persistence</i>
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Description

Given the incidence vector of a vertex subset, calculates either the persistence probability or the null-adjusted persistence of cluster C . This function is polymorphic: it automatically detects the input type and accepts either a vertex vector (accompanied by an edge list) or directly an igraph object.

Usage

```
local_persistence(x, ...)

## Default S3 method:
local_persistence(x, edge_list, weights = NULL, cluster, H0 = 0, ...)

## S3 method for class 'igraph'
local_persistence(x, cluster, H0 = 0, ...)
```

Arguments

<code>x</code>	An integer or character vector representing the graph vertices, OR an object of class <code>igraph</code> .
<code>...</code>	Additional arguments passed to specific methods (e.g., <code>edge_list</code> , <code>weights</code> , <code>cluster</code> , <code>H0</code>).
<code>edge_list</code>	Integer matrix with two columns representing the graph edge list.
<code>weights</code>	Numeric vector of edge weights. If <code>NULL</code> , all weights default to 1.
<code>cluster</code>	Binary incidence vector of the cluster: $x_i = 1$ if i in C , 0 otherwise.

H_0 Selects the quality measure. If NULL, the persistence probability is used. If 0 (default), the null-adjusted persistence (NAP). If a value in $(0, 1]$, the scaled null-adjusted persistence (Scaled-NAP, $sNAP_\alpha$), with scaling exponent α equal to H_0 .

Value

Numeric scalar: the persistence probability when $H_0 = \text{NULL}$, the null-adjusted persistence (NAP) when $H_0 = 0$, or the scaled null-adjusted persistence (Scaled-NAP, $sNAP_\alpha$, with $\alpha = H_0$) when H_0 is in $(0, 1]$.

Examples

```
library(scalednap)

# --- EXAMPLE 1: Standard input (vectors and matrices) ---
edg <- c(1, 2, 1, 3, 1, 4, 2, 3, 3, 4, 4, 5, 5, 6, 5, 7, 6, 7)
edge_list <- matrix(edg, ncol = 2, byrow = TRUE)
vertex <- c(1, 2, 3, 4, 5, 6, 7)
cluster_bin <- c(1, 1, 1, 1, 0, 0, 0)
local_persistence(x = vertex, edge_list = edge_list, cluster = cluster_bin)

# --- EXAMPLE 2: igraph input ---
if (requireNamespace("igraph", quietly = TRUE)) {
  g <- igraph::make_ring(10)
  cluster_bin <- c(rep(1, 5), rep(0, 5))
  local_persistence(g, cluster = cluster_bin)
}
```

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