

Package ‘xactonomial’

July 30, 2025

Type Package

Title Inference for Functions of Multinomial Parameters

Version 1.2.0

Date 2025-07-30

URL <https://sachsmc.github.io/xactonomial/>

BugReports <https://github.com/sachsmc/xactonomial/issues/>

Description We consider the problem where we observe k vectors (possibly of different lengths), each representing an independent multinomial random vector. For a given function that takes in the concatenated vector of multinomial probabilities and outputs a real number, this is a Monte Carlo estimation procedure of an exact p-value and confidence interval. The resulting inference is valid even in small samples, when the parameter is on the boundary, and when the function is not differentiable at the parameter value, all situations where asymptotic methods and the bootstrap would fail. For more details see Sachs, Fay, and Gabriel (2025) <[doi:10.48550/arXiv.2406.19141](https://doi.org/10.48550/arXiv.2406.19141)>.

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Encoding UTF-8

SystemRequirements Cargo (Rust's package manager), rustc >= 1.70

Suggests knitr, rmarkdown, testthat (>= 3.0.0)

VignetteBuilder knitr

RoxygenNote 7.3.2

Config/rextendr/version 0.3.1.9001

Config/testthat/edition 3

Depends R (>= 4.2)

NeedsCompilation yes

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Repository CRAN

Date/Publication 2025-07-30 08:00:02 UTC

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calc_multinom_probs *Calculate multinomial probabilities*

Description

Calculate multinomial probabilities

Usage

```
calc_multinom_probs(sar, logt, logc, d, n, nt)
```

Arguments

sar	The unrolled matrix containing the portion of the sample space to sum over
logt	The vector of candidate theta values, as sampled from the null space
logc	The vector of log multinomial coefficients see log_multinom_coef
d	The total dimension, $\sum(d_j)$
n	The sample size
nt	The number of candidate theta values

Value

A vector of probabilities

Examples

```

ospace_3_5 <- sspace_multinom(3, 5)
calc_multinom_probs(sspace_3_5, sample_unit_simplexn(3, 10),
  apply(matrix(sspace_3_5, ncol = 3, byrow = TRUE), 1, log_multinom_coef, sumx = 5), 3, 5, 10)

```

calc_prob_null	<i>Calculate probability for given parameters</i>
----------------	---

Description

Given a set of candidate parameter vectors, the enumerated sample space, and a logical vector with the same number of elements of the sample space, compute the probability for each element of the sample space and take the sum.

Usage

```
calc_prob_null(theta_cands, SSpacearr, logC, II)
```

Arguments

theta_cands	A matrix with samples in the rows and the parameters in the columns
SSpacearr	A matrix with the sample space for the given size of the problem
logC	log multinomial coefficient for each element of the sample space
II	logical vector of statistic for elements of sample space statistic being more extreme than the observed statistic

Value

A numeric vector of probabilities

Examples

```

ospace_3_5 <- matrix(sspace_multinom(3, 5), ncol = 3, byrow = TRUE)
theta_cands <- matrix(sample_unit_simplexn(3, 10), ncol = 3, byrow = TRUE)
calc_prob_null_fast(theta_cands, ospace_3_5,
  apply(sspace_3_5, 1, log_multinom_coef, sumx = 5), II = 1:21 > 12)
# same as below but faster
calc_prob_null(theta_cands, ospace_3_5,
  apply(sspace_3_5, 1, log_multinom_coef, sumx = 5), II = 1:21 > 12)

```

calc_prob_null_fast *Calculate probability for given parameters*

Description

Given a set of candidate parameter vectors, the enumerated sample space, and a logical vector with the same number of elements of the sample space, compute the probability for each element of the sample space and take the sum.

Usage

```
calc_prob_null_fast(theta_cands, SSpacearr, logC, II)
```

Arguments

theta_cands	A matrix with samples in the rows and the parameters in the columns
SSpacearr	A matrix with the sample space for the given size of the problem
logC	log multinomial coefficient for each element of the sample space
II	logical vector of statistic for elements of sample space statistic being more extreme than the observed statistic

Value

A numeric vector of probabilities

Examples

```
sspace_3_5 <- matrix(sspace_multinom(3, 5), ncol = 3, byrow = TRUE)
theta_cands <- matrix(sample_unit_simplexn(3, 10), ncol = 3, byrow = TRUE)
calc_prob_null_fast(theta_cands, sspace_3_5,
  apply(sspace_3_5, 1, log_multinom_coef, sumx = 5), II = 1:21 > 12)
# same as below but faster
calc_prob_null(theta_cands, sspace_3_5,
  apply(sspace_3_5, 1, log_multinom_coef, sumx = 5), II = 1:21 > 12)
```

calc_prob_null_gradient
Gradient of the multinomial likelihood sum

Description

Gradient of the multinomial likelihood sum

Usage

```
calc_prob_null_gradient(theta_cands, SSpacearr, II)
```

Arguments

`theta_cands` A matrix with samples in the rows and the parameters in the columns

`SSpacearr` A matrix with the sample space for the given size of the problem

`II` logical vector of statistic for elements of sample space statistic being more extreme than the observed statistic

Value

A matrix the same dimension as `theta_cands`

Examples

```
calc_prob_null_gradient(t(c(.28, .32, .4)),
matrix(c(2, 2, 1, 1, 2, 2, 0, 3, 2), ncol = 3),
rep(TRUE, 3))

# numerically
testenv <- new.env()
testenv$SSpacearr <- matrix(c(2, 2, 1, 1, 2, 2, 0, 3, 2), ncol = 3)
testenv$thistheta <- c(.28, .32, .4)
numericDeriv(quote(sum(exp((.colSums(t(SSpacearr) * log(thistheta), m = 3, n = 3))))),
theta = "thistheta", rho = testenv, central = TRUE)
```

combine

Arrange all combinations of rows of two matrices

Description

Given X and Y, both matrices where the rows are counts of multinomial trials, produce all combinations rowwise, concatenate the rows into a new matrix, and calculate the log multinomial coefficients for the combination.

Usage

```
combine(X, Y)
```

Arguments

`X` Matrix 1

`Y` Matrix 2

Value

A list containing Sspace, the sample space (vectors of counts), and logC, a vector of the log multinomial coefficients.

Examples

```
slist_2_3 <- combineate(matrix(sspace_multinom(2, 5), ncol = 2, byrow = TRUE),
  matrix(sspace_multinom(3, 6), ncol = 3, byrow = TRUE))
```

 combineate2

Like [combinate](#) but adds on to previous call

Description

Like [combinate](#) but adds on to previous call

Usage

```
combineate2(X, Y)
```

Arguments

X	A list containing the elements Sspace (matrix), and logC (vector), the result of a call to combinate
Y	Matrix 2

Value

A list containing Sspace, the sample space (vectors of counts), and logC, a vector of the log multinomial coefficients.

Examples

```
slist_2_3 <- combineate(matrix(sspace_multinom(2, 5), ncol = 2, byrow = TRUE),
  matrix(sspace_multinom(3, 6), ncol = 3, byrow = TRUE))
```

```
sl_2_3_4 <- combineate2(slist_2_3, matrix(sspace_multinom(4, 3), ncol = 4, byrow = TRUE))
```

`itp_root`*Find a univariate root of the function f*

Description

This finds the value $x \in [a, b]$ such that $f(x) = 0$ using the one-dimensional root finding ITP method (Interpolate Truncate Project). Also see [itp](#).

Usage

```
itp_root(  
  f,  
  a,  
  b,  
  k1 = 0.1,  
  k2 = 2,  
  n0 = 1,  
  eps = 0.005,  
  maxiter = 100,  
  fa = NULL,  
  fb = NULL,  
  verbose = FALSE,  
  ...  
)
```

Arguments

<code>f</code>	The function to find the root of in terms of its first (one-dimensional) argument
<code>a</code>	The lower limit
<code>b</code>	The upper limit
<code>k1</code>	A tuning parameter
<code>k2</code>	Another tuning parameter
<code>n0</code>	Another tuning parameter
<code>eps</code>	Convergence tolerance
<code>maxiter</code>	Maximum number of iterations
<code>fa</code>	The value of $f(a)$, if NULL then will be calculated
<code>fb</code>	The value of $f(b)$, if NULL then will be calculated
<code>verbose</code>	Prints out information during iteration
<code>...</code>	Other arguments passed on to <code>f</code>

Value

A numeric vector of length 1, the root at the last iteration

References

I. F. D. Oliveira and R. H. C. Takahashi. 2020. An Enhancement of the Bisection Method Average Performance Preserving Minmax Optimality. *ACM Trans. Math. Softw.* 47, 1, Article 5 (March 2021), 24 pages. <https://doi.org/10.1145/3423597>

Examples

```
fpoly <- function(x) x^3 - x - 2 ## example from the ITP_method wikipedia entry
itp_root(fpoly, 1, 2, eps = .0001, verbose = TRUE)
```

log_multinom_coef *Calculate log of multinomial coefficient*

Description

Calculate log of multinomial coefficient

Usage

```
log_multinom_coef(x, sumx)
```

Arguments

x	Vector of observed counts in each cell
sumx	Total count

Value

The vector of log multinomial coefficients

Examples

```
S0 <- matrix(sspace_multinom(4, 6), ncol = 4, byrow = TRUE)
logC0 <- apply(S0, 1, log_multinom_coef, sumx=6)
```


pvalue_psi0

Compute a p value for the test of $\psi \leq \psi_0$ and/or $\psi \geq \psi_0$ **Description**

Compute a p value for the test of $\psi \leq \psi_0$ and/or $\psi \geq \psi_0$

Usage

```
pvalue_psi0(
  psi0,
  f_param,
  psi_hat,
  psi_obs,
  alternative = "two.sided",
  maxit,
  chunksize,
  p_target,
  SSpacearr,
  logC,
  d_k,
  f_is_vectorized = FALSE,
  theta_sampler = runif_dk_vects,
  ga = FALSE,
  ga_gfactor = 1,
  ga_lrate = 0.01,
  ga_restart_every = 10,
  warn = TRUE
)
```

Arguments

psi0	The null hypothesis value for the parameter being tested.
f_param	Function that takes in parameters and outputs a real valued number for each parameter. Can be vectorized rowwise for a matrix or not.
psi_hat	The vector of psi values at each element of the sample space
psi_obs	The observed estimate at the given data
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
maxit	Maximum number of iterations of the Monte Carlo procedure
chunksize	The number of samples to take from the parameter space at each iteration
p_target	If a p-value is found that is greater than p_target, terminate the algorithm early.
SSpacearr	The sample space matrix
logC	The log multinomial coefficients for each row of the sample space

d_k	The vector of dimensions
f_is_vectorized	Is f_param vectorized by row?
theta_sampler	Function to take samples from the <i>Theta</i> parameter space. Default is runif_dk_vects .
ga	Logical, if TRUE, uses gradient ascent.
ga_gfactor	Concentration parameter scale in the gradient ascent algorithm. A number or "adapt"
ga_lrate	The gradient ascent learning rate
ga_restart_every	Restart the gradient ascent after this number of iterations at a sample from
warn	If TRUE, will give a warning if no samples from the null space are found

Value

A vector with two p-values, one for the lower, and one for the greater

Examples

```

ospace_3_5 <- matrix(sspace_multinom(3, 5), ncol = 3, byrow = TRUE)
f_max <- function(theta) max(theta)
logC <- apply(sspace_3_5, 1, log_multinom_coef, sumx = 5)
psi_hat <- apply(sspace_3_5, 1, \(x) f_max(x / sum(x)))
pvalue_psi0(.3, f_max, psi_hat, .4, maxit = 10, chunksize = 100,
  p_target = 1, SSpacearr = sspace_3_5, logC = logC, d_k = 3, warn = FALSE)

```

rdirich_dk_vects	<i>Sample independently from Dirichlet distributions for each of d_k vectors</i>
------------------	--

Description

Sample independently from Dirichlet distributions for each of d_k vectors

Usage

```
rdirich_dk_vects(nsamp, alpha)
```

Arguments

nsamp	number of samples to take
alpha	List of vectors of concentration parameters

Value

A matrix with sum(d_k) columns and nsamp rows

Examples

```
rdirich_dk_vects(10, list(rep(1, 3), rep(1, 4), rep(1, 2)))
```

```
runif_dk_vects            Sample uniformly and independently from d_k simplices
```

Description

Sample uniformly and independently from d_k simplices

Usage

```
runif_dk_vects(d_k, nsamp)
```

Arguments

d_k	vector of vector lengths
nsamp	number of samples to take

Value

A matrix with $\text{sum}(d_k)$ columns and nsamp rows

Examples

```
runif_dk_vects(c(3, 4, 2), 10)
```

```
sample_unit_simplexn    Sample n times from the unit simplex in d dimensions
```

Description

Sample n times from the unit simplex in d dimensions

Usage

```
sample_unit_simplexn(d, n)
```

Arguments

d	the dimension
n	the number of samples to take uniformly in the d space

Value

The grid over Theta, the parameter space. To be converted to a matrix with d columns and n rows

Examples

```
matrix(sample_unit_simplexn(3, 10), ncol = 3, byrow = TRUE)
```

sspace_multinom	<i>Enumerate the multinomial sample space</i>
-----------------	---

Description

Enumerate the multinomial sample space

Usage

```
sspace_multinom(d, n)
```

Arguments

d	The dimension
n	The sample size

Value

A vector enumerating the sample space, to be converted to a matrix with d columns and $\text{choose}(n + d - 1, d - 1)$ rows

Examples

```
matrix(sspace_multinom(3, 5), ncol = 3, byrow = TRUE)
```

sspace_multinom_slow	<i>Enumerate the sample space of a multinomial</i>
----------------------	--

Description

We have d mutually exclusive outcomes and n independent trials. This function enumerates all possible vectors of length d of counts of each outcome for n trials, i.e., the sample space. The result is output as a matrix with d columns where each row represents a possible observation. See [sspace_multinom](#) for a faster implementation using Rust.

Usage

```
sspace_multinom_slow(d, n)
```

Arguments

d	Dimension
n	Size

Value

A matrix with d columns

Examples

```
d4s <- sspace_multinom_slow(4, 8)
stopifnot(abs(sum(apply(d4s, 1, dmultinom, prob = rep(.25, 4))) - 1) < 1e-12)
```

xactonomial	<i>Improved inference for a real-valued function of multinomial parameters</i>
-------------	--

Description

We consider the k sample multinomial problem where we observe k vectors (possibly of different lengths), each representing an independent sample from a multinomial. For a given function $\tau(\theta)$ which takes in the concatenated vector of multinomial probabilities θ and outputs a real number, we are interested in computing a p-value for a test of $\tau(\theta) = \psi \geq \psi_0$, and constructing a confidence interval for ψ .

Usage

```
xactonomial(
  data,
  f_param,
  statistic = NULL,
  psi0 = NULL,
  alternative = c("two.sided", "less", "greater"),
  psi_limits,
  theta_null_points = NULL,
  p_target = 1,
  conf_int = TRUE,
  conf_level = 0.95,
  itp_maxit = 10,
  itp_eps = 0.005,
  p_value_limits = NULL,
  maxit = 50,
  chunksize = 500,
  theta_sampler = runif_dk_vects,
  ga = TRUE,
  ga_gfactor = "adapt",
```

```

    ga_lrate = 0.01,
    ga_restart_every = 10,
    seed = 503
)

```

Arguments

<code>data</code>	A list with k elements representing the vectors of counts of a k -sample multinomial
<code>f_param</code>	Function that takes in parameters and outputs ψ , a real valued number for each parameter. Can be vectorized rowwise for a matrix or not.
<code>statistic</code>	Function that takes in a matrix with data vectors in the rows, and outputs a vector with the number of rows in the matrix. If NULL, will be inferred from <code>f_param</code> by plugging in the empirical proportions.
<code>psi0</code>	The null hypothesis value for the parameter being tested.
<code>alternative</code>	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
<code>psi_limits</code>	A vector of length 2 giving the lower and upper limits of the range of $\tau(\theta)$
<code>theta_null_points</code>	An optional matrix where each row is a θ value that gives $f_param(\theta) = \psi_0$. If this is supplied and $\psi_0 =$ one of <code>psi_limits</code> , then a truly exact p-value will be calculated.
<code>p_target</code>	If a p-value is found that is greater than <code>p_target</code> , terminate the algorithm early.
<code>conf_int</code>	If TRUE, calculates a confidence interval by inverting the p-value function
<code>conf_level</code>	A number between 0 and 1, the confidence level.
<code>itp_maxit</code>	Maximum iterations to use in the ITP algorithm. Only relevant if <code>conf_int = TRUE</code> .
<code>itp_eps</code>	Epsilon value to use for the ITP algorithm. Only relevant if <code>conf_int = TRUE</code> .
<code>p_value_limits</code>	A vector of length 2 giving lower bounds on the one-sided p-values corresponding to $\psi_0 = \psi_limits$, with <code>alternative = "less"</code> and <code>"greater"</code> , respectively. Only relevant if <code>conf_int = TRUE</code> . See examples.
<code>maxit</code>	Maximum number of iterations of the Monte Carlo procedure
<code>chunksize</code>	The number of samples to take from the parameter space at each iteration
<code>theta_sampler</code>	Function to take samples from the <i>Theta</i> parameter space. Default is <code>runif_dk_vects</code> . Must be a function of two parameters <code>d_k</code> a vector of dimensions, and <code>chunksize</code> the number of samples to take, and return a matrix with $\text{sum}(d_k)$ columns and <code>chunksize</code> rows. See examples.
<code>ga</code>	Logical, if TRUE, uses gradient ascent.
<code>ga_gfactor</code>	Concentration parameter scale in the gradient ascent algorithm. A number or "adapt"
<code>ga_lrate</code>	The gradient ascent learning rate
<code>ga_restart_every</code>	Restart the gradient ascent after this number of iterations at a sample from <code>theta_sampler</code>
<code>seed</code>	Seed for the random number generator. Can be set to NULL in which case no seed is set.

Details

Let T_j be distributed Multinomial $_{d_j}(\theta_j, n_j)$ for $j = 1, \dots, k$ and denote $\mathbf{T} = (T_1, \dots, T_k)$ and $\boldsymbol{\theta} = (\theta_1, \dots, \theta_k)$. The subscript d_j denotes the dimension of the multinomial. Suppose one is interested in the parameter $\psi = \tau(\boldsymbol{\theta}) \in \Psi \subseteq \mathbb{R}$. Given a sample of size n from \mathbf{T} , say $\mathbf{X} = (X_1, \dots, X_k)$, which is a vector of counts obtained by concatenating the k independent count vectors, let $G(\mathbf{X})$ denote a real-valued statistic that defines the ordering of the sample space. The default choice of the statistic is to estimate $\boldsymbol{\theta}$ with the sample proportions and plug them into $\tau(\boldsymbol{\theta})$. This function calculates a p value for a test of the null hypothesis $H_0 : \psi \neq \psi_0$ for the two sided case, $H_0 : \psi \leq \psi_0$ for the case alternative = "greater", and $H_0 : \psi \geq \psi_0$ for the case alternative = "less". We make no assumptions and do not rely on large sample approximations. It also optionally constructs a $1 - \alpha$ percent confidence interval for ψ . The computation is somewhat involved so it is best for small sample sizes. The calculation is done by sampling a large number of points from the null parameter space Θ_0 , then computing multinomial probabilities under those values for the range of the sample space where the statistic is as or more extreme than the observed statistic given data. It is basically the definition of a p-value implemented with Monte Carlo methods. Some options for speeding up the calculation are available.

Value

An object of class "htest", which is a list with the following elements:

estimate The value of the statistic at the observed data

p.value The p value

conf.int The upper and lower confidence limits

null.value The null hypothesis value provided by the user

alternative The type of test

method A description of the method

data.name The name of the data object provided by the user

p.sequence A list with two elements, p.null and p.alt containing the vector of p values at each iteration for the less than null and the greater than null. Used for assessing convergence.

Specifying the function $\tau(\cdot)$

This function is the `f_param` argument and should be a function that either: 1) takes a vector of length `sum(d_j)` (the total number of bins) and outputs a single number, or 2) takes a matrix with number of columns equal to `sum(d_j)`, and arbitrary number of rows and outputs a vector with length equal to the number of rows. In other words, `psi` can be not vectorized or it can be vectorized by row. Writing it so that it is vectorized can speed up the calculation. See examples.

Boundary issues

It is required to provide `psi_limits`, a vector of length 2 giving the smallest and largest possible values that the function `psi` can take, e.g., `c(0, 1)`. If the null hypothesis value `psi0` is at one of the limits, it is often the case that sampling from the null parameter space is impossible because it is a set of measure 0. While it may have measure 0, it is not empty, and will contain a finite set of points. Thus you should provide the argument `theta_null_points` which is a matrix where the rows contain the finite set (sometimes 1) of points $\boldsymbol{\theta}$ such that $\tau(\boldsymbol{\theta}) = \psi_0$. There is also an argument

called `p_value_limits` that can be used to improve performance of confidence intervals around the boundary. This should be a vector of length 2 with the p-value for a test of $\psi_0 \leq \psi_limits[1]$ and the p-value for a test of $\psi_0 \geq \psi_limits[2]$. See examples.

Optimization options

For p-value calculation, you can provide a parameter `p_target`, so that the sampling algorithm terminates when a p-value is found that exceeds `p_target`. The algorithm begins by sampling uniformly from the unit simplices defining the parameter space, but alternatives can be specified in `theta_sampler`. By default gradient ascent (`ga = TRUE`) is performed during the p-value maximization procedure, and `ga_gfactor` and `ga_lrate` control options for the gradient ascent. At each iteration, the gradient of the multinomial probability at the current maximum `theta` is computed, and a step is taken to `theta + lrate * gradient`. Then for the next iteration, a set of `chunksize` samples are drawn from a Dirichlet distribution with parameter `ga_gfactor * (theta + ga_lrate * gradient)`. If `ga_gfactor = "adapt"` then it is set to $1 / \max(\theta)$ at each iteration. The ITP algorithm `itp_root` is used to find roots of the p-value function as a function of the `psi0` value to get confidence intervals. The maximum number of iterations and epsilon can be controlled via `itp_maxit`, `itp_eps`.

References

Sachs, M.C., Gabriel, E.E. and Fay, M.P., 2024. Exact confidence intervals for functions of parameters in the k-sample multinomial problem. arXiv preprint arXiv:2406.19141.

Examples

```
tau_ba <- function(theta) {
  theta1 <- theta[1:4]
  theta2 <- theta[5:8]
  sum(sqrt(theta1 * theta2))
}
data <- list(T1 = c(2,1,2,1), T2 = c(0,1,3,3))
xactonomial(data, tau_ba, psi_limits = c(0, 1), psi0 = .5,
  conf_int = FALSE, maxit = 15, chunksize = 200)

# vectorized by row
tau_ba_v <- function(theta) {
  theta1 <- theta[,1:4, drop = FALSE]
  theta2 <- theta[,5:8, drop = FALSE]
  rowSums(sqrt(theta1 * theta2))
}
data <- list(T1 = c(2,1,2,1), T2 = c(0,1,3,3))
xactonomial(data, tau_ba_v, psi_limits = c(0, 1), psi0 = .5,
  conf_int = FALSE, maxit = 10, chunksize = 200)

# example of using theta_null_points
# psi = 1/3 occurs when all probs = 1/3
tau_max <- function(pp) {
  max(pp)
}
```



```
data <- list(c(13, 24, 13))

xactonomial(data, tau_max, psi_limits = c(1 / 3, 1), psi0 = 1/ 3,
  conf_int = FALSE, theta_null_points = t(c(1/3, 1/3, 1/3)))

## in this case using p_value_limits improves confidence interval performance

xactonomial(data, tau_max, psi_limits = c(1 / 3, 1), psi0 = 1/ 3,
  conf_int = TRUE, theta_null_points = t(c(1/3, 1/3, 1/3)),
  p_value_limits = c(.1, 1e-8))

## specifying theta_sampler

dirich_sampler <- function(d_k, chunksize){
  rdirich_dk_vects(chunksize, list(1:4 + 1))
}

xactonomial(list(1:4),tau_max,
  psi_limits = c(0.25,1), psi0 = .5, conf_int = FALSE,
  theta_sampler = dirich_sampler)
```

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